

# Single-coil Design Approach for Dual-band Near-field Coupled Resonators

Lai Ly Pon

Southern University College,  
Malaysia

Corresponding author: llpon@sc.edu.my

**Abstract:** With the adoption of single coil approach, printed spiral resonator design strategy for near-field wireless energy transfer is presented. A pair of symmetrical resonators operating at high frequency band specifically 6.78 MHz and 13.56 MHz is designed. Simulated power transfer efficiency (PTE) of over 88% are obtained for both frequencies when coupled spiral resonators separated at a distance of 25 mm is integrated with hybrid compensation network topology. The variance of PTE between both frequencies is about 0.04.

**Keywords:** impedance matching, power transfer efficiency, printed spiral resonator, single-coil, wireless energy transfer.

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## 1. INTRODUCTION

Near field wireless energy transfer system operating at more than one frequency band exceed its single band predecessor by offering the prospect of simultaneous energy and data transfer as well as dual-mode energy transfer functionalities. One of the commonly used performance metrics in wireless energy transfer is power transfer efficiency (PTE). There is a tendency that PTE for either one of the concerned frequencies greatly exceed the other. On the other hand, this shortcoming will be ideal for simultaneous energy and data functionalities provided that maximum transfer efficiency and sufficient bandwidth allocation are not compromised.

Multi-coil [1], [2], [3] and single-coil [4], [5], [6] design approaches are used to achieve the aforementioned intentions. Nevertheless, similar with any front-end designs, both methods come with their respective downsides. Designing separate resonators as in the case of multi-coil approach often viewed as a better option since stand-alone resonators with its corresponding impedance matching networks is capable of realizing highest transfer efficiency as demonstrated in [7] with the implementation of two circular defected ground structure (DGS). Even though DGS offers miniaturized design, the lowest resonance frequency to date is 280 MHz [8].

Hence, this paper presents a design approach for a dual-band printed spiral resonator with two resonant frequencies at  $f_1$ , 6.78 MHz and  $f_2$ , 13.56 MHz with the aim of accomplishing minimum transfer efficiency variance between first and second resonant frequency. This paper is organized as follows. Section 2 presents the design method while Section 3 discusses results obtained. A comparison between proposed design in this work and

other published work is presented. Finally, this paper is concluded in Section 4.

## 2. DESIGN METHOD

There are two predominant stages in the front-end design of wireless energy transfer system namely resonator design and impedance transformation network. Full-wave electromagnetic simulator, CST Microwave Studio is employed in the design of spiral resonator. Design and enhancement steps are portrayed in Figure 1. Selection of optimal axial distance,  $z_{OP}$  is equally important in order to extract maximum magnetic field excitation [9], [10]. The optimal axial distance is found by

$$z_{OP} = 0.3931 d_o \quad (1)$$

where  $d_o$  is outermost diameter length of loop. Since calculated optimal distance is 23.6 mm, 25 mm is selected before performing any optimization.

Geometrical constraints specified are number of turns, width and spacing of conductive trace. Dimension of the proposed double-sided design is 70 mm by 75 mm with FR-4 substrate thickness of 1.6 mm. Conductor thickness opted is 0.07 mm. Thicker conductor will aid in the reduction of resistance. A total of seven turns are designed with three and four loops etched on top and bottom layer of the substrate respectively. Optimization is performed to enhance geometrical layout as this remains as one of essential rectification techniques for dual-band resonator designs [11]. Other parameter properties are detailed in Table 1 while the proposed design layout is depicted in Figure 2.

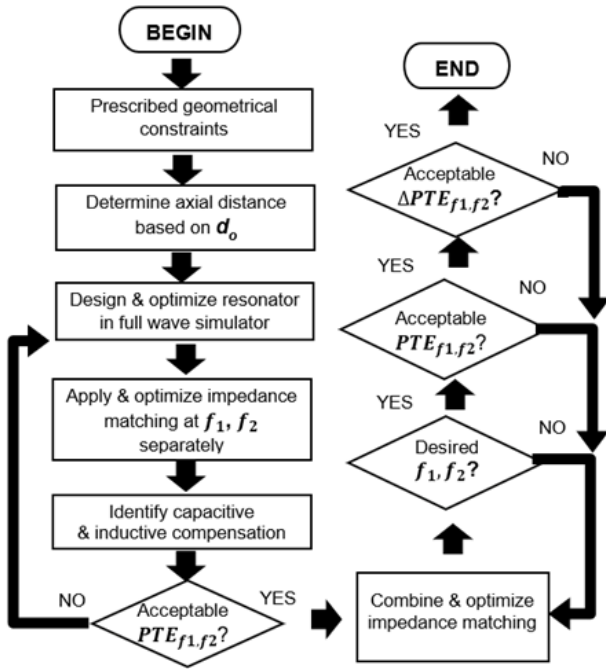


Figure 1. Single coil approach design strategy

Table 1. Parameters of resonator design

| Symbols  | Parameters                             | Value (mm) |
|----------|--|------------|
| $d_o$    | Outermost side length                  | 60         |
| $d_i$    | Innermost side length                  | 10.35      |
| $w_{ot}$ | Outermost conductor width top layer    | 2.5        |
| $w_{it}$ | Innermost conductor width top layer    | 1.3        |
| $s_{ot}$ | Outermost spacing top layer            | 4.6        |
| $s_{it}$ | Innermost spacing top layer            | 6.9        |
| $w_{ob}$ | Outermost conductor width bottom layer | 2.5        |
| $w_{ib}$ | Innermost conductor width bottom layer | 1.25       |
| $s_{ob}$ | Outermost spacing bottom layer         | 3.475      |
| $s_{ib}$ | Innermost spacing bottom layer         | 8.3        |

Following geometrical layout refinement on resonator design, the subsequent steps involve impedance matching. Simultaneous conjugate matching is critical in ensuring maximum power transfer between a pair of coupled resonators [12]. There are numerous ways to implement impedance matching using lumped elements as reactive compensation. Single capacitive compensation,  $C_n$  can be derived from equation (2) where  $f_r$  and  $L$  denote desired resonance frequency and loop inductance.

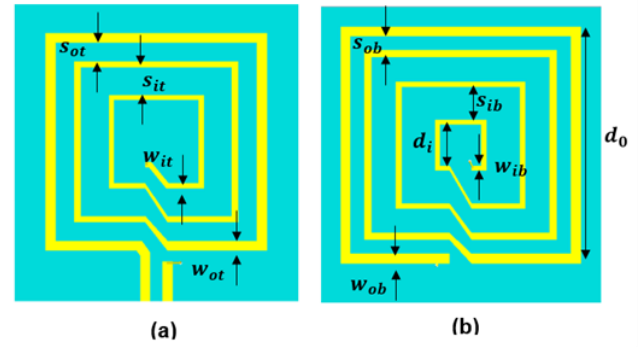


Figure 2. Single coil approach design layout: a) Top view, b) Bottom view

$$C_n = ((2\pi f_r)^2 L)^{-1} \quad (2)$$

Double capacitive compensation can be achieved by connecting a series and parallel capacitors at the transmitting and receiving resonators. As shown in Figure 3, this compensation network topology is also commonly known as  $L$ -matching. Capacitive values can be determined from inbuilt search algorithm available in full wave finite element simulator.

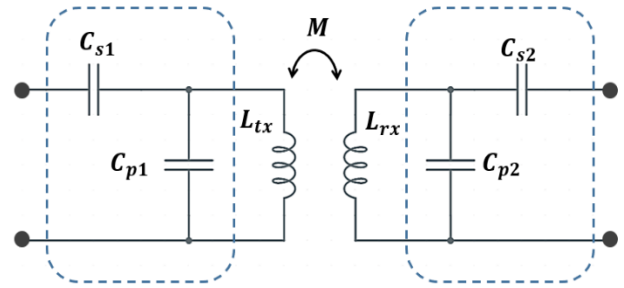


Figure 3. Equivalent schematic of double capacitive compensation

Apart from double capacitive compensation, parallel resonant circuit is applied in order to realize peak transfer efficiency at dual resonance frequency. Both parallel resonant  $L - C$  tank and series resonant  $L - C$  branch have been implemented in [13]. However, there is a considerable variance of transfer efficiency between lower and higher resonance frequency. In this design, parallel resonant circuit and double capacitive compensation are proposed. Table 2 lists the separate initial and optimized values of reactive components. Figure 4 depicts equivalent schematic of proposed design. Optimization is performed after combining both impedance matching methods. The initial and optimized values of reactive components are shown in Table 3.

Table 2. Separate initial and optimized impedance matching

| Resonance Frequency | Parameters | Initial      | Optimized    |
|---------------------|------------|--------------|--------------|
| $f_1$               | $C_{s1}$   | 27 pF        | 158.57 pF    |
|                     | $C_{p1}$   | 252 pF       | 132.48 pF    |
| $f_2$               | $L_1$      | 2.14 $\mu$ H | 3.65 $\mu$ H |
|                     | $C_1$      | 64.36 pF     | 101.57 pF    |

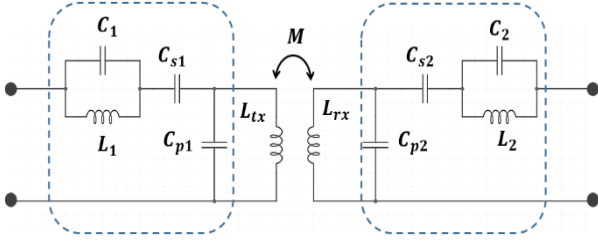


Figure 4. Equivalent schematic of proposed design

Table 3. Combined initial and optimized impedance matching

| Parameters | Initial      | Optimized    |
|------------|--------------|--------------|
| $L_1$      | 3.65 $\mu$ H | 1.86 $\mu$ H |
| $C_1$      | 101.57 pF    | 31.64 pF     |
| $C_{s1}$   | 158.57 pF    | 87.21 pF     |
| $C_{p1}$   | 132.48 pF    | 146.96 pF    |
| $L_2$      | 3.65 $\mu$ H | 2.69 $\mu$ H |
| $C_2$      | 101.57 pF    | 25.24 pF     |
| $C_{s2}$   | 158.57 pF    | 87.70 pF     |
| $C_{p2}$   | 132.48 pF    | 102.06 pF    |

### 3. RESULT AND DISCUSSION

Performance of wireless energy transfer link can be evaluated through  $S$ -parameters. Figure 5 shows simulated input reflection coefficient,  $S_{11}$  and transmission coefficient,  $S_{21}$ . Two resonances are achieved at targeted frequencies, 6.78 MHz and 13.56 MHz. Power transfer efficiency is derived from the magnitude of transmission coefficient,  $S_{21}$  as given by Equation (3) [14].

$$PTE (\%) = 100(|S_{21}|^2) \quad (3)$$

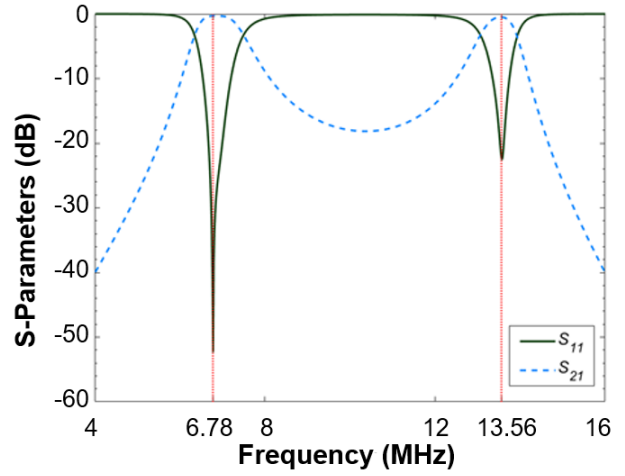


Figure 5. Simulated S-parameters plot of single coil design approach for dual-band near-field coupled resonators

As shown in Figure 6, PTE obtained at 6.78 MHz and 13.56 MHz are 93% and 89% respectively. The average transfer efficiency computed is 91%. Equation (4) is employed to compute the difference between transfer efficiency at each targeted resonance frequency which is represented by  $\Delta PTE_{f_1, f_2}$ . Table IV lists the computed average and variance of transfer efficiency. Result obtained indicates that single-coil-approach integrated with hybrid compensation network topology is possible in decreasing the gap between PTE of first resonance and second resonance frequency. Another advantage of employing single-coil approach besides intercoupling decrement [13] is geometrical area reduction. Table V summarizes comparison with other published works.

$$\Delta PTE_{f_1, f_2} = |PTE_{f_1} - PTE_{f_2}| \quad (4)$$

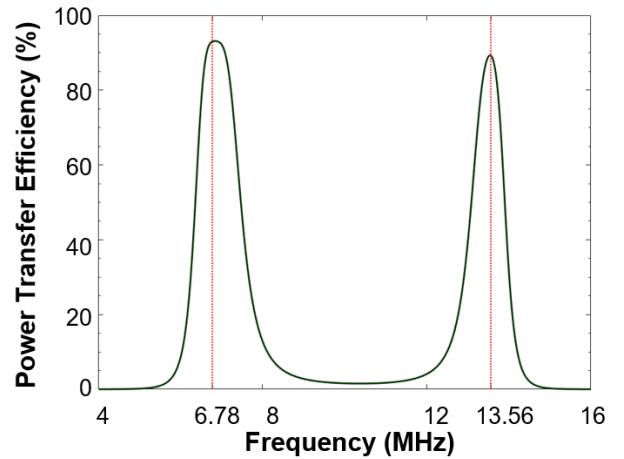


Figure 6. Simulated PTE at fixed axial distance of 25 mm

Table 4. Simulated Power Transfer Efficiency

| d (mm) | $PTE_{f_1}$ (%) | $PTE_{f_2}$ (%) | $PTE_{av}$ (%) | $\Delta PTE_{f_1, f_2}$ |
|--------|-----------------|-----------------|----------------|-------------------------|
| 25     | 93              | 89              | 91             | 0.04                    |

Table 5. Comparison with other published works

| Ref          | Approach    | $f_1$       | $f_2$        | $PTE_{f_1}$<br>(%) | $PTE_{f_2}$<br>(%) | $PTE_{av}$<br>(%) | Variance,<br>$\Delta PTE_{f_1, f_2}$ | $z$<br>(mm) | TX size<br>( $mm^2$ ) | Link         | Impedance<br>Matching                           |
|--------------|-------------|-------------|--------------|--------------------|--------------------|-------------------|--------------------------------------|-------------|-----------------------|--------------|---|
| [2]          | Multi-coil  | 200<br>kHz  | 6.78<br>MHz  | 70.6               | 78                 | 74.3              | 0.07                                 | 25          | 11125                 | Asymmetrical | Hybrid<br>compensation                          |
| [15]         | Multi-coil  | 6.78<br>MHz | 13.56<br>MHz | 72.34              | 74.02              | 73.18             | 0.02                                 | 30          | 7200                  | Symmetrical  | Capacitive<br>compensation                      |
| [8]          | Multi-coil  | 280<br>MHz  | 490<br>MHz   | 91.2               | 79.4               | 85.3              | 0.12                                 | 6           | 400                   | Symmetrical  | Capacitive<br>compensation                      |
| [4]          | Single-coil | 200<br>kHz  | 6.78<br>MHz  | 55                 | 74                 | 64.5              | 0.19                                 | 50          | 10350                 | Asymmetrical | Hybrid<br>compensation                          |
| [5]          | Single-coil | 6.78<br>MHz | 13.56<br>MHz | 49.14              | 37.21              | 43.175            | 0.12                                 | 200         | 19200                 | Asymmetrical | Coupling loop<br>and capacitive<br>compensation |
| This<br>work | Single-coil | 6.78<br>MHz | 13.56<br>MHz | 93                 | 89                 | 91                | 0.04                                 | 25          | 5250                  | Symmetrical  | Hybrid<br>compensation                          |

#### 4. CONCLUSION

This paper is intended to serve as a simplified design guideline for near-field coupled resonators using single-coil approach. Targeted dual resonance frequency with minimal variation ratio of 0.04 between each transfer efficiency is accomplished with integration of hybrid compensation network topology acquired based on numerical simulation. Single-coil approach proposed is indicative that dual-mode resonator implementation is viable without necessitating additional structures such as two standalone resonators or repeaters.

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